## DEPARTMENT OF MATHEMATICS S.F

## Vision

To empower women globally competent with human values and ethics acquiring academic and entrepreneurship skills through holistic education.

## Mission

1. To create opportunities which will ensure academic excellence in critical thinking, humanistic and scientific inquiry.
2. To develop application oriented courses with the necessary input of values.
3. To create a possible environment for innovation, team spirit and entrepreneurial leadership.
4. To form young women of competence, commitment and compassion.

## Programme Educational Objectives (PEO)

| PEO 1 | The graduates will apply appropriate theory and scientific knowledge to <br> participate in activities that support humanity and economic development <br> nationally and globally, developing as leaders in their fields of expertise. |
| :---: | :--- |
| PEO 2 | The graduates pursue lifelong learning and continuous improvement of the <br> knowledge and skills with the highest professional and ethical standards. |
| PEO 3 | The graduates will demonstrate the ability to utilize effectively the variety of <br> teaching techniques and class room strategies and develop confidence to appear <br> for competitive examinations and occupy higher levels of academic and <br> administrative fields. |

## Programme Outcomes (PO)

| PO | Upon completion of the B.Sc. Degree Programme, the graduates <br> will be able to: |
| :---: | :--- |
| PO - 1 | equip students with hands on training through various courses to enhance <br> entrepreneurship skills. |
| PO - 2 | impart communicative skills and ethical values. |
| PO - 3 | face challenging competitive examinations that offer rewarding careers in <br> science and education. |
| PO - 4 | apply the acquired scientific knowledge to face day to day needs and reflect <br> upon green initiatives to build a sustainable environment. |

## Programme Specific Outcomes (PSO)

| PSO | Upon completion of the B.Sc. Degree Programme, the <br> graduates will be able to: | PO addressed |
| :--- | :--- | :--- |
| PSO - 1 | acquire a strong foundation in various branches of mathematics to <br> formulate real life problems into mathematical models | PO 4 |
| PSO - 2 | apply the mathematical knowledge and skills to develop problem <br> solving skills cultivating logical thinking and face competitive <br> examinations with confidence. | PO 3, 4 |
| PSO - 3 | develop entrepreneurial skills based on ethical values, become <br> empowered and self-dependent in society. | PO 1,2 |
| PSO - 4 | enhance numerical ability and address problems in <br> interdisciplinary areas which would help in project and field works. | PO 1 |
| PSO - 5 | pursue scientific research and develop new findings with global <br> impact using latest technologies. | PO 4 |

# III UG <br> Teaching Plan 

## Complex Analysis

| Semester |  |  | : |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name of the $\mathbf{C}$ | our |  |  | mpl | Analysis |  |  |  |  |  |
| Course code |  |  |  | 20 |  |  |  |  |  |  |
| CourseCode | L | T | P | S | Credits | Inst. <br> Hours | Total |  |  |  |
|  |  |  |  |  |  |  |  | $\begin{array}{r} \text { CI } \\ \text { Tot } \\ \hline \end{array}$ | $\mathbf{E x}$ |  |
| MC2061 | 5 | 1 | - | - | 5 | 6 | 90 | 25 | 75 | 100 |

## Objectives:

1. To introduce the basic concepts of differentiation and integration of Complex functions
2. To apply the related concepts in higher studies

## Course Outcomes

| CO | Upon completion of this course the students will be able to | PSO <br> Addressed | CL |
| :---: | :--- | :---: | :--- |
| CO - 1 | understand the geometric representation of mappings | PSO - 1 | K2(U) |
| CO - 2 | use differentiation rules to compute derivatives and express <br> complex- differentiable functions as power series | PSO - 4 | K5(E) |
| CO - 3 | compute line integrals by using Cauchy's integral theorem <br> and formula | PSO - 3 | K5(E) |
| CO - 4 | identify the isolated singularities of a function and determine <br> whether they are removable, poles or essential | PSO - 1 | K2(U) |
| CO - 5 | evaluate definite integrals by using residues theorem | PSO - 5 | K6(C) |

Total contact hours: 90 (Including lectures, assignments and tests)

| Unit | Module | Topics | Lectur <br> ehours | Cogni tive level | Learning Outcomes | Pedagogy | Assess ment/ evaluat ion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Differentiability |  |  |  |  |  |  |
|  | 1 | Differentiability definitions and theorems | 3 | $\begin{aligned} & \mathrm{K} 1(\mathrm{R}) \\ & \mathrm{K} 2(\mathrm{U}) \end{aligned}$ | To analyze the basic properties of differentiability | Lecture using videos | Recall <br> basic <br> definitions <br> on <br> differentia <br> bility <br> Con |
|  | 2 | Cauchy Riemann equations, theorems and examples, Alternate forms of C.R equations theorems and problems | 7 | K2(U) | To get necessary and sufficient condition for differentiability | Blending method | Concept definitions <br> Questionin g <br> Formative <br> Assessmen <br> t |
|  | 3 | Analytic functions definition and problems | 5 | K4(An) | To discuss some properties of an analytic function | Lecture using PPT | Class test, <br> Simple definitions ,examples, MCQ Test |
|  | 4 | Harmonic functions, definitions, theorems and problems | 7 | K3(Ap) | To find an analytic functions | Lecture with Group Discussion | Recall steps, Questionin g and Home Assignme nt |
| II | Transformations |  |  |  |  |  |  |
|  | 1 | Bilinear transformations, | 7 | K2(U) | To determine the image of given | Lecture with PPT | Concept definitions |

$\left.\begin{array}{|c|c|l|l|l|l|l|}\hline & & \begin{array}{l}\text { elementary } \\ \text { transformation and } \\ \text { cross ratio }\end{array} & & & \begin{array}{l}\text { region under } \\ \text { bilinear } \\ \text { transformation }\end{array} & \begin{array}{c}\text {, } \\ \text { Questionin } \\ \text { g }\end{array} \\ \text { Formative } \\ \text { Assessmen } \\ \text { t }\end{array}\right]$

|  | 3 | Cauchy's integral formula - theorems and problems | 5 | K3(Ap) | To evaluate integrals | Lecture with Group Discussion | Recall steps, Open book test |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | Taylor's and Laurent's Series |  |  |  |  |  |  |
|  | 1 | Taylor's seriesTaylor's theorem and problems | 5 | $\begin{gathered} \mathrm{K} 2(\mathrm{U}), \\ \mathrm{K} 4(\mathrm{An}) \end{gathered}$ | To expand the given function as Taylor's series | Lecture <br> method, <br> Group <br> Discussion, <br> Lecture <br> using videos <br> and <br> Problem <br> solving. | Concept definitions <br> Questionin g <br> Formative Assessmen t |
|  | 2 | Laurent's Series Laurent's theorem and problems | 5 | K2(U) | To expand the given function as Laurent'sseries | Group Discussion, Lecture using videos and Problem solving. | Class test, Simple definitions ,examples, MCQ Test Formative Assessmen t |
|  | 3 | Zeros of analytic functions definition and problems | 3 | K4(An) | To determine the zerosof an analytic functions | Lecture using PPT and Peer teaching Lecture withGroup Discussion | Class test, Simple definitions ,examples, MCQ Test Assignme nt |
|  | 4 | Singularities definitions and examples | 1 | K3(Ap) | To find the singularity ofa given function | Lecture withGroup Discussion and Peer teaching | Simple <br> definitions <br> ,examples, <br> Solving <br> problems, <br> MCQ, Slip <br> Test |
| V |  |  |  | Cauchy | esidues |  |  |


| 1 | Residues definition, lemmas and problems | 5 | K2(U) | To find the residue of a given function | Lecture using PPT and Peer teaching | Concept <br> definitions <br> , <br> Questionin <br> g <br> Formative <br> Assessmen <br> t <br> Evaluation <br> through <br> short test. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | Cauchy's residue theorem - theorems and examples | 3 | K4(An) | To apply Cauchy's residue theorem by evaluating the integrals | Lecture with Illustration, Group Discussion, Lecture using PPT and Peer teaching | Concept definitions <br> Questionin g <br> Formative Assessmen t |
| $3$ | Evaluation of definite integrals method and problems | 5 | K3(Ap) | To evaluate the definiteintegrals by using the given method | Problem solving, Lecture with PPT, <br> Lecture with Illustration | Class test, <br> Simple definitions ,examples, MCQ Test |

Course Focussing on Employability/ Entrepreneurship/ Skill Development: Employability
Activities (Em/En/SD): Solving the Problems, Group discussion, Seminar, Online Assignment
Course Focussing on Cross Cutting Issues (Professional Ethics/ Human Values/Environment Sustainability/ Gender Equity): Nil

Activities related to Cross Cutting Issues: Nil
Assignment: Bilinear transformations, elementary transformation and cross ratio

Seminar Topic: Cauchy's integral formula, theorems and problems

## Part A

1. What are the necessary conditions for a function $f(z)$ to be analytic in a given domain?
a) Existence of partial derivatives
b) Existence of Cauchy-Riemann equations
c) Satisfying the Laplace equation
d) All of the above
2. For an analytic function $f(z)$, which of the following statements is true?
a) It is always a real-valued function
b) Its derivative is not unique
c) It satisfies the Cauchy-Riemann equations
d) It has a singularity at every point
3. What is the cross ratio of four distinct complex numbers $z 1, z 2, z 3, z 4$ ?
a) $(z 2-z 1)(z 4-z 3) /(z 3-z 1)(z 4-z 2)$
b) $(z 2-z 1) /(z 4-z 3)$
c) $(z 1-z 3)(z 2-z 4) /(z 1-z 4)(z 2-z 3)$
d) $(z 3-z 1) /(z 4-z 2)$
4. Which theorem guarantees the existence of anti derivatives for holomorphic functions?
a) Cauchy's Residue Theorem
b) Fundamental Theorem of Algebra
c) Maximum Modulus Theorem
d) Cauchy's Integral Theorem
5. In a Laurent series expansion, if all the coefficients corresponding to negative powers of $\left(z^{-a}\right)$ are zero, what type of singularity does the function have at $z=a$ ?
a) Essential singularity
b) Removable singularity
c) Pole
d) Branch point

## Part B

6. Consider the function $f(z)=3 z^{2}+2 i$. Determine whether this function is analytic, and if so, find its derivative.
7. Given the bilinear transformation $w=\frac{2 z+i}{3 z-2 i}$, find the expression for $z$ in terms of $w$. Also, map the points $z_{1}=1$ and $z_{2}=-i$ under this transformation and express the results in terms of $w$.
8. Evaluate the following complex integral $\int_{C} \frac{e^{z}}{z-1} d z$ where $C$ is the circle $|z|=2$ traversed counterclockwise.
9. Find the Taylor series expansion of the function $f(z)=\frac{1}{z^{2}-4}$ centered at $z=0$. Determine the radius of convergence and identify any singularities.
10. Use the Residue theorem to evaluate the following integral $\oint_{C} \frac{\cos (z)}{(z-1)(z-2)}$ where $C$ is the positively oriented circle $|z|=3$.

## Part C

11. State and prove Taylor's Theorem.
12. Prove that any bilinear transformation can be expressed as product of translation, rotation, magnification and inversion.
13. Prove that the cross ratio is preserved by a Bilinear transformation.
14. State and prove residue theorem.
15. Find the bilinear transformation which maps the points $z_{1}=2, z_{2}=i, z_{3}=-2$ onto $w_{1}$ $=1, \mathrm{w}_{2}=\mathrm{i}, \mathrm{w}_{3}=-1$ respectively.


Course Instructor
Dr. P.C. Priyanka Nair

Head of the Department
Dr. S. Kavitha

## Mechanics

## Department : Mathematics (SF) <br> Class : III B.Sc. Mathematics (SF)

Title of the Course : Major Core XI- Mechanics
$\begin{array}{ll}\text { Semester } & : \quad \text { VI } \\ \text { Course Code } & : \\ & \text { MC2062 }\end{array}$

| Course Code | $\mathbf{L}$ | $\mathbf{T}$ | $\mathbf{P}$ | Credits | Inst. Hours | Total | Mours |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

## Objectives:

1. To visualize the application of Mathematics in Physical Sciences
2. To develop the capacity to predict the effects of force and motion

## Course Outcomes

| CO | Upon completion of this course the students will be able <br> to | PSO <br> Addressed | CL |
| :--- | :--- | :---: | :---: |
| CO -1 | calculate the reactions necessary to ensure static equilibrium | PSO - 2 | K2(U) |
| CO - 2 | apply the principles of static equilibrium to particles and <br> rigid bodies | PSO - 4 | K3(Ap) |
| CO - 3 | understand the ways of distributing loads | PSO - 5 | K6 (C) |
| CO - 4 | identify internal forces and moments of a rigid body | PSO - 3 | K3(Ap) |
| CO -5 | apply the basic principles of projectiles into real world <br> problems | PSO - 2 | K3(Ap) |


| CO - 6 | classify the laws of friction | PSO - 4 | K4(An) |
| :--- | :--- | :--- | :--- |

Total contact hours: 90 (Including lectures, assignments and tests)

| Unit | $\underset{\mathbf{e}}{\text { Modul }}$ | Topics | Teaching <br> Hours | Cognitive level | Pedagogy | Assessme nt/ evaluation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Forces Acting at a Point, Parallel Forces and Moments |  |  |  |  |  |
|  | 1 | Introduction to types of Forces and equilibrium of forces | 1 | K2(U) | Introductory session | Simple definitions, Recall basic definitions |
|  | 2 | Forces Acting at a <br> Point:Resultant and Components - Sample cases of finding the resultant, Analytical expression for the resultant of two forces acting at a point, Triangle forces, Perperndicular Triangular forces, Converse of the Trigangle of Forces, The Polygon of Forces, Lami's Theorem, Problems based on Lami's Theorem | 3 | $\begin{aligned} & \text { K2(U) } \\ & \text { K3(Ap) } \end{aligned}$ | Interactive <br> PPT using <br> Gamma AI <br> tool | Quiz using slido |
|  | 3 | Resultant of two like parallel forces, two unlike and unequal parallel forces, Resultant of number of parallel forces, equilibrium of three coplanar parallel forces | 3 | $\begin{aligned} & \text { K3(Ap) } \\ & \text { K6 (C) } \end{aligned}$ | Lecture using Chalk and talk | Evaluation through slip test |


|  | 4 | Moment of a force, Geometrical representation, Varignon's theorem of moments | 4 | K3(Ap) | Flipped <br> Classroom | Group <br> Discussion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5 | Generalised theorem of moments, Problems based on Varignon's theorem of moments, Generalised theorem of moments | 4 | K3(Ap) | Lecture with interactive video | MCQ Using <br> Nearpod |
| II | Couples, Coplanar Forces |  |  |  |  |  |
|  | 1 | Couples - Equilibrium oftwo couples - <br> Representation of a couple by a vector Resultant of coplanar couples - Resultant of couple and a force Problems based on Couples, Introduction and reduction of any number of coplanar forces, Analytical proof | 4 | $\begin{aligned} & \mathrm{K} 2(\mathrm{U}) \\ & \mathrm{K} 3(\mathrm{Ap}) \end{aligned}$ | Interactive <br> PPT using <br> Gamma AI <br> tool | Oral test |
|  | 2 | Conditions for forces to reduce a single force or couple, Change of the base point \& Equation tothe line of action of the resultant | 3 | $\begin{aligned} & \mathrm{K} 2(\mathrm{U}) \\ & \mathrm{K} 3(\mathrm{Ap}) \end{aligned}$ | Lecture with Interactive video | Quizziz |
|  | 3 | Problems based on reduction of number of coplanar forces | 2 | K3(Ap) | Demonstratio <br> n | Slip test |
|  | 4 | Problems based on forces to reduce a single force or couple | 3 | K3(Ap) | Blended <br> Classroom | MCQ |
|  | 5 | Problems based on Equation to the line of action of the resultant | 3 | K3(Ap) | Flipped <br> Classroom | MCQ using <br> Nearpod |
| III |  |  |  | Frictio |  |  |


|  | 1 | Introduction, Statical, Dynamical, Limiting friction and Laws of friction, Coefficient of friction, Angle of friction, Cone of friction | 4 | $\begin{aligned} & \mathrm{K} 2(\mathrm{U}) \\ & \mathrm{K} 4(\mathrm{An}) \end{aligned}$ | Lecture with interactive PPT | Quiz using Slido |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2 | Equilibrium of a particle on a rough inclined plane, Equilibrium of a body on a rough inclined plane under a force parallel to the plane, Equilibrium of a body on a rough inclined planeunder any force | 3 | $\begin{aligned} & \mathrm{K} 2(\mathrm{U}) \\ & \mathrm{K} 4(\mathrm{An}) \end{aligned}$ | Evaluative Learning | Formative <br> Assessment <br> Test I |
|  | 3 | Problems based on Coefficient of friction, angle of friction | 4 | $\begin{aligned} & \mathrm{K} 2(\mathrm{U}) \\ & \mathrm{K} 4(\mathrm{An}) \end{aligned}$ | Blended <br> Classroom | Assignment |
|  | 4 | Problems based on Equilibrium of a particle on a rough inclined plane and equilibrium of a body on a rough inclined plane under a force parallel to the plane | 4 | $\begin{aligned} & \mathrm{K} 2(\mathrm{U}) \\ & \mathrm{K} 4(\mathrm{An}) \end{aligned}$ | Flipped <br> Classroom | Group Discussion |
| IV | Projectiles |  |  |  |  |  |
|  | 1 | Fundamental principles, Path of a projectile, Characteristics of the motion of a projectile | 3 | K3(Ap) | Lecture with interactive PPT using Gamma AI tool | Evaluation through short test |
|  | 2 | Path of a projectile at a certain height above the ground, Problems based on Path of a projectile, Problems based on Characteristics of the motion of a projectile | 4 | K3(Ap) | Demonstratio <br> n | Practical <br> Exercises |


|  |  |  | Maximum horizontal <br> range, Two possible <br> directions of <br> projection,Problems <br> based on maximum <br> horizontal <br> range and Two <br> possibledirections of <br> projection | 4 | K2(U) <br> K3(Ap) |
| :---: | :---: | :---: | :--- | :--- | :--- |


|  | paths by reweighting <br> and related Lemma |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Course Focusing on Employability/Entrepreneurship/Skill Development : Skill Development

Activities(Em/En/SD) : 1. Evaluation through short test, Quiz competition
2. Model Making, Puzzles

Assignment: Preparation of quiz questions, Velocity of the projectile
Seminar Topic: Friction, Velocities in a centralorbit - Two - fold problems in central orbits.
Course Focussing on Cross Cutting Issues (Professional Ethics/ Human Values/Environment Sustainability/ Gender Equity): Nil

Activities related to Cross Cutting Issues: Nil

## Sample questions

## Part-A

1.State Lami's Theorem
2.If the force tends to turn the body in a clockwise direction, its moment is said to be
3.The conditions of equilibrium depend only on
a) couples
a) resultant
a)forces
e)none of these
4.Co-efficient of friction is $\qquad$ .
a) FR
b) $F / R$
c) $\mu \mathrm{F}$
d) $\mu R$
5.Greatest height attained by a projectile is $\qquad$ .
6. Force of friction depends on
a) weight of the object
b) speed
c) Time
d) None of these

## Part B

1. $A B C$ is a given triangle Forces $P, Q, R$ acting along the lines $O A, O B, O C$ are in equilibrium. Prove that $P: Q: R=\cos \frac{A}{2}: \cos \frac{B}{2}: \cos \frac{C}{2}$ if O is the in centre of the triangle.
2. Forces $\mathrm{P}, 4 \mathrm{P}, 2 \mathrm{P}, 6 \mathrm{P}$ act along the sides $\mathrm{AB}, \mathrm{BC}, \mathrm{CD}, \mathrm{DA}$ of a square of side a . Show that the equation to the line of action of the resultant is $2 x-y+6 a=0$ with $A B$ and $A D$ as axes of coordinates.
3. State the laws of friction
4. A particle is projected horizontally from a point at a certain height above the ground show that the path described by it is a parabola.
5. If $h$ and $h^{1}$ be the greatest heights in the two paths of a projectile with a given velocity for a given range $R$. Prove that $R=4 \sqrt{h h^{1}}$.
Part - C
1.State and prove Lami's theorem
6. State and prove Varigons theorem of moments.
3.Forces $F_{1}, F_{2}, F_{3}, F_{4}, F_{5}, F_{6}$ act along the sides of a regular hexagon taken in order. Show that they will be in equilibrium if (i) $F_{1}+F_{2}+F_{3}+F_{4}+F_{5}+F_{6}=0$ and (ii) $F_{1}-F_{4}=F_{3}-F_{6}=F_{5}-F_{2}$. 4. A uniform ladder is in equilibrium with one end resting on the ground and the other against a vertical wall; if the ground and wall be both rough, the coefficients of friction being $\mu$ and $\mu^{1}$ respectively, and if the ladder be on the point of slipping at both ends, show that $\theta$, the inclination of the ladder to the horizon is given by $\tan \theta=\frac{1-\mu \mu^{1}}{2 \mu}$
7. Show that the path of a projectile is a parabola.
8. Show that the greatest height which a particle with initial velocity v can reach on a vertical wall at a distance a from the point of projection is $\frac{v^{2}}{2 g}-\frac{g a^{2}}{2 v^{2}}$. Prove also that the greatest height above the point of projection attained by the particle in its flight is $V^{61} / 2 g\left(v^{4}+g^{2} a^{2}\right)^{\text {. }}$


## Course Instructor

Dr. S.Kavitha


## Head of the Department

Dr. S.Kavitha

## Number Theory

| Semester |  |  | : VI |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name of the Course |  |  | : Number Theory |  |  |  |  |  |  |  |
| Course code |  |  | : MC2063 |  |  |  |  |  |  |  |
| CourseCode | L | T | P | S | Credits | Inst. Hours | Total <br> Hours | Marks |  |  |
|  |  |  |  |  |  |  |  | CIA | Ext | Total |
| MC2063 | 4 | 1 | - | - | 4 | 5 | 75 | 25 | 75 | 100 |

## Objectives:

1. To introduce the fundamental principles and concepts in Number Theory
2. To apply these principles in other branches of Mathematics

## Course Outcomes

| CO | Upon completion of this course the students will be able to | PSO <br> Addressed | CL |
| :--- | :--- | :--- | :--- |
| CO - 1 | express the concepts and results of divisibility of integers <br> effectively | PSO - 1 | U |
| CO -2 | construct mathematical proofs of theorems and find counter <br> examples for false statements | PSO - 2 | Ap |
| CO - 3 | collect and use numerical data to form conjectures about the <br> integers | PSO - 5 | Ap |
| CO -4 | understand the logic and methods behind the major proofs in <br> Number Theory | PSO - 4 | An |


| CO -5 | solve challenging problems related to Chinese remainder <br> theorem effectively | PSO - 3 | E |
| :--- | :--- | :---: | :---: |
| CO - 6 | build up the basic theory of the integers from a list of axioms | PSO - 1 | U |

Total contact hours:90 (Including lectures, assignments and tests)

| Unit | Modul <br> e | Topics | $\begin{gathered} \hline \text { Teachi } \\ \text { ng } \\ \text { hours } \\ \hline \end{gathered}$ | Cognitive Level | Pedagogy | Assessment/ evaluation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Divisibility Theory in the Integers |  |  |  |  |  |
|  | 1 | Preliminaries-Numbers ,integers, Divisors and Divisibility Theory in the Integers | 3 | K1(R) | Lecture with Illustration | Evaluation through appreciative inquiry |
|  | 2 | The Division Algorithm theorem and its applications | 3 | K2(U) | Lecture using PPT | Evaluation through quizzes and discussions. |
|  | 3 | The greatest common divisor and least common multiple | 3 | K3(Ap) | Lecture using videos | Evaluation Through SlipTest |
|  | 4 | Euclid's lemma <br> and Euclidean <br> Algorithm | 3 | K4(An) | Problem Solving | Evaluation through Quiz andTest |
| II | Diophantine Equation |  |  |  |  |  |
|  | 1 | The Diophantine <br> Equation $a x+b y=c$ | 3 | K2(U) | $\begin{gathered} \text { Lecture with } \\ \text { chalk and } \\ \text { talk } \end{gathered}$ | Evaluation Through discussions. |
|  | 2 | Primes and their Distribution. | 3 | K2(U) | Problem <br> Solving | Evaluation through Appreciative inquiry |


|  | 3 | The fundamental theorem of arithmetic | 3 | K3(Ap) | Lecture using PPT PPT | Evaluation through <br> Formative <br> Assessment <br> Test |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4 | The Sieve of Eratosthenes | 3 | K4(An) | Group <br> Discussion | Evaluation through <br> Formative Assessment Test |
| III | Theory of Congruences |  |  |  |  |  |
|  | 1 | Theory of Congruences | 3 | K2(U) | Lecture with Illustration | Evaluation through appreciative inquiry |
|  | 2 | Basic properties of congruences | 3 | K3(Ap) | Flipped Class | Evaluation through quizzes and discussions |
|  | 3 | Linear congruences and The Chinese remainder theorem. | 3 | K4(An) | $\begin{gathered} \text { Lecture using } \\ \text { PPT } \end{gathered}$ | Evaluation through SlipTest |
|  | 4 | Problems based on Chinese remainder theorem | 3 | K3(Ap) | Discussion with Illustration | $\begin{aligned} & \text { Evaluation } \\ & \text { through Quiz } \\ & \text { andTest } \end{aligned}$ |
| IV | Pseudo primes |  |  |  |  |  |
|  | 1 | Fermat's Little theorem and Pseudo primes | 2 | K2(U) | Lecture with PPT <br> Illustration | Evaluation through discussions |
|  | 2 | Absolute Pseudo primes | 3 | K3(Ap) | Flipped Class | Evaluation through appreciative inquiry |
|  | 3 | Wilsons theorem | 3 | K3(Ap) | Lecture with Illustration | Evaluation through <br> Formative <br> Assessment Test |
|  | 4 | Quadratic Congruence | 3 | K5(E) | Group <br> Discussion | Evaluation through SlipTest |
| V | Number Theoretic Functions |  |  |  |  |  |


|  | 1 | Number Theoretic <br> Functions | 3 | K2(U) | Lecture with <br> Illustration | Evaluation <br> through <br> discussions. |
| :---: | :---: | :--- | :---: | :--- | :--- | :---: |
| 2 | 3 | The sum and number of <br> divisors | 3 | K3(Ap) | Lecture and <br> Group <br> Discussion | Evaluation <br> Through <br> Assignment |
| The Mobius Inversion |  |  |  |  |  |  |
| formula. | 3 | K4(An) | Evaluation <br> through |  |  |  |
| 4 | The greatest integer <br> function | 3 | K5(E) | Flipped Class <br> FormativeAssess <br> ment <br> Test |  |  |

Course Focussing on Employability/ Entrepreneurship/ Skill Development : Skill Development Activities (Em/En/SD): Solving the Problems, Group discussion, Seminar, Assignment

Course Focussing on Cross Cutting Issues (Professional Ethics/ Human Values/Environment Sustainability/ Gender Equity): Nil

Activities related to Cross Cutting Issues: Nil
Assignment : The sum and number of divisors, The Mobius Inversion formula.

Seminar Topic: Basic properties of congruences, Problems based on Chinese remainder
Theorem

## Sample Questions

PART-A

1. Find $\operatorname{gcd}(12378,3024)$ using Euclidean algorithm.
2. The $\operatorname{gcd}(12,30)$ is
a) 7
b)6
c) 3
d) 1
3. A solution of the Diophantine equation is $\qquad$
4. An equation of the form $a x \equiv b(\bmod n)$ is called as $\qquad$ .
a) Congruence
b) Modular congruence
c) Linear Congruence
5. $2^{31} \equiv$ $\qquad$ (mod11)
(a) 11
(b) 31
c) 1
(d) 2

## PART-B

1. ABC is a given triangle Forces $\mathrm{P}, \mathrm{Q}, \mathrm{R}$ acting along the lines $\mathrm{OA}, \mathrm{OB}, \mathrm{OC}$ are in equilibrium.

Prove that $P: Q: R=\cos \frac{A}{2}: \cos \frac{B}{2}: \cos \frac{C}{2}$ if O is the in centre of the triangle.
2. A body is projected with a velocity of $98 \mathrm{~m} / \mathrm{sec}$ in a direction making an angle $\tan ^{-1} 3$ with the horizon; Show that it rises to a vertical height of 441 meters and that its time of flight is about 19 secs. Find also horizontal range through the point of projection. ( $\mathrm{g}=9.8 \mathrm{~m} / \mathrm{sec}^{2}$ ).
3. If $v_{1} \& v_{2}$ be the velocities of a projectile at the ends of a focal chord of its path and

U is the velocity at the vertex prove that $\mathrm{v}_{1}{ }^{-2}+\mathrm{v}_{2}{ }^{-2}=\mathrm{U}^{-2}$.
4. State and prove Fermat's theorem.
5. Show that the system of linear congruence $a x+b r \equiv r(\bmod n), c x+d y \equiv s(\operatorname{modn})$ has a unique solution modulo n whenever $\operatorname{gcd}(\mathrm{ad}-\mathrm{bc}, \mathrm{n})=1$.

## PART-C

1. $A$ and $B$ are two fixed points on a horizontal line at a distance $C$ apart. Two fine light strings AC and BC of lengths b and a respectively support a mass at
C. Show that the tensions of the strings are in the ratio $b\left(a^{2}+c^{2}-b^{2}\right): a\left(b^{2}+c^{2}-a^{2}\right)$.
2. Prove that equation of the path of the projectile is a parabola.
3. State and prove Chinese RemainderTheorem.
4. Prove that the number $\sqrt{2}$ is irrational.
5. State and prove Wilson's theorem. Is the converse true?


Dr. S. Kavitha

## Head of the Department



Dr. J. Ness Golden Flower

## Linear Programming

| Department | $:$ | Mathematics (SF) |
| :--- | :--- | :--- |
| Class | $:$ | III B.Sc. Mathematics (SF) |
| Title of the Course | $:$ | Core XIII: Linear Programming |
| Semester | $:$ | VI |
| Course Code | $:$ | MC2064 |


| Course Code | L | T | $\mathbf{P}$ | Credits | Inst. Hours | Total <br> Hours | Marks |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | CIA | External | Total |
| MC2064 | 5 | - | - | 4 | 5 | 75 | 25 | 75 | 100 |

## Objectives:

1. To formulate real life problems into mathematical problems.
2. To solve life oriented and decision making problems by optimizing the objective function.

## Course Outcomes

| CO | Upon completion of this course, the <br> students will be able to: | PSO <br> addressed | Cognitive level |
| :--- | :--- | :--- | :---: |
| CO -1 | understand the methods of optimization and to <br> solve the problems | PSO - 1 | K2 (U) |
| CO - 2 | explain what is an LPP | PSO - 1 | K2 (U) |
| CO - 3 | define how to formulate an LPP with linear <br> constraints | PSO -1 | K1 (R) |
| CO - 4 | maximize the profit, minimize the cost, <br> minimize the time in transportation problem, <br> Travelling salesman problem, Assignment <br> problem | PSO - 3 | K3 (Ap) |


| CO - 5 | identify a problem in your locality, formulate <br> it as an LPP and solve | PSO -4 | K6 (C) |
| :--- | :--- | :---: | :---: |

Total contact hours: 75 (Including lectures, assignments and tests)

| Unit | Module | Topics | Teaching Hours | Cognitive level | Pedagogy | Assessment/ <br> Evaluation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I |  |  |  |  |  |  |
|  | 1 | Formulation of LPP, <br> Mathematical <br> Formulation of LPP, <br> Solution of LPP |  | K2 (U) | Introductory session, Lecture with illustration | Questioning, Recall steps, concept with examples |
|  | 2 | Graphical method | 4 | K3 (Ap) | Flipped classroom | Group discussion |
|  | 3 | Algorithm for Simplexmethod | 1 | K2 (U) | Lecture with illustration | Slip Test |
|  | 4 | Simplex method problems | 3 | K3 (Ap) | PPT | Quiz using slido |
|  | 5 | Algorithm for Big-M <br> Method, Big-M <br> Method problems | 4 | K2 (U) | Lecture Method | concept explanations |


| II |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | Two phase method Phase I: Solving auxiliary LPP using Simplex method | 4 | K3 (Ap) | Computational thinking | Evaluation through short test |
|  | 2 | Phase II: finding optimal basic feasible solution | 3 | K3 (Ap) | Flipped classroom | concept definitions, concept with examples |
|  | 3 | Duality in L.P.P, Primal, Formation of dual L.P.P, Matrix form of primal and its dual, Fundamental theorem of duality | 3 | K2 (U) | Blended learning | Quiz using Nearpod |
|  | 4 | Dual Simplex Algorithm, Dual simplex problems | 3 | K2 (U) | Problem solving | Slip Test, Quiz using google forms |
|  | 5 | Degeneracy and cycling in L.P.P. | 2 | K3 (Ap) | Lecture using videos | Brainstorming, Formative Assessment I |
| III |  |  |  |  |  |  |
|  | 1 | Mathematical formulation of Transportation Problems, Dual of a Transportation Problem | 3 | K1 (R) | Demonstrative | concept with examples, Questioning |
|  | 2 | Solution of a <br> Transportation <br> Problem, <br> North-West corner rule | 3 | K3 (Ap) | Lecture Method | Evaluation through short test |
|  | 3 | Row minima method, Column minima method, Least Cost Method | 3 | K2 (U) | PPT | Group discussion |
|  | 4 |  | 3 | K2 (U) | Lecture with illustration | Brain storming |


|  |  | Vogel's <br> Approximation Method |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5 | Degeneracy in Transportation Problems | 3 | K3 (Ap) | Problem solving | Slip Test |
| IV |  |  |  |  |  |  |
|  | 1 | Assignment <br> Problems, <br> Mathematical formulation, Solution <br> to Assignment <br> Problems | 5 | K3 (Ap) | Introductory session | concept with examples |
|  | 2 | Hungarian Algorithm for solving AssignmentProblem | 5 | K3 (Ap) | Problem solving | concept explanations, Quiz using Slido |
|  | 3 | Travelling Salesman Problem | 5 | K3 (Ap) | Computational thinking | Group discussion, Assignment |
| V |  |  |  |  |  |  |
|  | 1 | Introduction to Sequencing | 3 | K1 (R) | Lecture Method | concept with examples |
|  | 2 | Processing n jobs in two machines | 4 | K3 (Ap) | Problem solving | Slip Test |
|  | 3 | Processing n jobs in m machines | 4 | K3 (Ap) | Problem solving | Quiz using google forms, Seminar |
|  | 4 | Processing two jobs in $m$ machines | 4 | K3 (Ap) | Problem solving | Quiz using <br> Mentimeter, <br> Formative <br> Assessment II |

Course Focussing on Employability/ Entrepreneurship/ Skill Development: Entrepreneurship Activities (Em/En/SD): Identify a problem in the locality, formulate it as an LPP and solve it.

Course Focussing on Cross Cutting Issues (Professional Ethics/ Human Values/Environment Sustainability/ Gender Equity): Nil

Activities related to Cross Cutting Issues: Nil
Assignment: Travelling Salesman Problem
Seminar Topic: Processing $n$ jobs in $m$ machines

## Sample questions

## Part A

1. A basic solution is said to be $\qquad$ if none of the basic variable is zero.
(a) optimal
(b) degenerate
(c) non-degenerate
(d) feasible
2. In Two phase method, the solution is obtained in $\qquad$ phases.
3. State True or False:

If the primal problem is of maximizing type then the dual problem is of minimizing type.
4. The assignment problem is said to be balanced if $\qquad$ .
5. State True or False:

No machine may process more than one job simultaneously for sequencing problems.

## Part B

1. An egg contains 6 units of Vitamin A per gram and 7 units of Vitamin B per gram and costs 12 paise per gram. Milk contains 8 units of Vitamin A and 12 units of Vitamin B per gram and costs 20 paise per gram. The daily minimum requirements of Vitamin $A$ and Vitamin B are 100 units and 120 units. Find the optimal product mix. Formulate a LP model for the above problem.
2. Write the algorithm of Two Phase Method.
3. Using Least Cost Method, find a basic feasible solution to the following transportation problem.

|  | $\mathrm{W}_{1}$ | $\mathrm{~W}_{2}$ | $\mathrm{~W}_{3}$ | $a_{i}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~F}_{1}$ | 8 | 10 | 12 | 900 |
| $\mathrm{~F}_{2}$ | 12 | 13 | 12 | 1000 |
| $\mathrm{~F}_{3}$ | 14 | 10 | 11 | 1200 |


| $b_{j}$ | 1200 | 1000 | 900 | 3100 |
| :--- | :--- | :--- | :--- | :--- |

4. Solve the following Assignment problem

|  | A | B | C |
| :---: | :---: | :---: | :---: |
| X | 19 | 28 | 31 |
| Y | 11 | 17 | 16 |
| Z | 12 | 15 | 13 |

5. Write the algorithm to find the optimum sequence for n jobs in 2 machines.

## Part C

1. Solve the following LPP by Big-M method:

Minimize $z=60 x_{1}+80 x_{2}$ subject to
$20 x_{1}+30 x_{2} \geq 900$
$40 x_{1}+30 x_{2} \geq 1200$
$x_{1}, x_{2} \geq 0$.
2. Explain Dual Simplex algorithm.
3. Solve the following transportation problem

|  | C | D | E | Availability |
| :---: | :---: | :---: | :---: | :---: |
| A | 3 | 7 | 3 | 6 |
| B | 2 | 3 | 9 | 8 |
| Requirement | 4 | 7 | 3 | 14 |

4. A travelling salesman has to visit 5 cities. He wishes to start from a particular city, visit each city once and return to his starting point. Cost of travelling from one city to another it shown in the table below. Find the least cost route.

|  | A | B | C | D | E |
| :--- | :--- | :--- | :--- | :--- | :--- |
| A | $\infty$ | 4 | 10 | 14 | 2 |
| B | 12 | $\infty$ | 6 | 10 | 4 |
| C | 16 | 14 | $\infty$ | 8 | 14 |
| D | 24 | 8 | 12 | $\infty$ | 10 |


|  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| E | 2 | 6 | 4 | 14 | $\infty$ |

5. Write the algorithm to find the optimum sequence for n jobs in m machines.


Head of the Department: Dr.S.Kavitha


Course Instructor: Dr.C.Jenila

## Astronomy

| Class | $:$ III B.Sc Mathematics |
| :--- | :--- |
| Title of the course | : Major: Astronomy |
| Semester | $:$ VI |
| Name of the Course | : Astronomy |
| Course code | : MC2065 |


| Course |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| code | L

## Objectives:

1. To introduce space science and to familiarize the important features of theplanets, sun, moon and stellar universe
2. To predict lunar and solar eclipses and study the seasonal changes

## Course Outcomes

| CO | Upon completion of this course the students will be <br> able to | PSO <br> Addressed | Cognitive <br> level |
| :--- | :--- | :--- | :--- |
| CO -1 | define the spherical trigonometry of the celestial sphere | PSO - 4 | K3 |
| CO - 2 | discuss the Kepler's laws | PSO -4 | K3 |
| CO - 3 | calculate the motion of two particles relative to the <br> common mass centre | PSO - 3 | K3 \& K5 |


| CO -4 | interpret latitude and longitude and apply this to find the <br> latitude and longitude of a particular place | PSO - 2 | K2 |
| :--- | :--- | :---: | :---: |
| CO -5 | distinguish between Geometric Parallax and Horizontal <br> Parallax | PSO -4 | K4 |

Total Contact Hours:90 (Includinglectures,assignmentsand tests)

| Unit | Module | Topics | Teaching <br> Hours | Cognitive level | Pedagogy | Assessment/Ev <br> aluation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Celestialsphere |  |  |  |  |  |
|  | 2 | Spherical <br> trigonometry(only the <br> fourformulae)- <br> Celestialsphere | 3 | K2(U) | Lecturelllustrati <br> on | Simple definitions, <br> Recall basic <br> concepts |
|  | 3 | Diurnalmotion- <br> SiderealTime | 3 | K4(An) | Problem solving | oral,test |


|  | 4 | Dip ofHorizon | 4 | K2(U) | Blended <br> learning Fo | FormativeAssessme nt Test I |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5 | Twilight, Duration ofTwilight, Twilight throughout the night,Shortest Twilight. | 4 | K4(An) | Seminar | Quiz |
| III |  |  |  |  |  |  |
|  | 1 | Geocentric parallax Parallax, Effects of Geocentric parallax | 3 | K3(Ap) | Lecture with Illustration | Simple definitions |
|  | 2 | Changes in R.A andDeclination of a bodydue to GeocentricParallax | 4 | K2(U) | Lecture using videos | Solving problems |
|  | 3 | Angular diameter Equatorialhorizontal parallax | 4 | K4(An) | Flipped classroom | MCQ using slido |
|  | 4 | HeliocentricParallax, Effect of HeliocentricParallax | 3 | K3(Ap) | Blended learning | Formative Assessment Test I |
|  | 5 | To find the effectofParallax on theLongitudeandLatitudeof aStar-Parsec | 4 | K2(U) | Lecturelllustration | OnlineAssignment |
| IV | Kepler's laws |  |  |  |  |  |
|  | 1 | Kepler'slawsEccentricityofEarth'sorbit | 3 | K4(An) | LectureIllustration | O OralTest |
|  | 2 | Verification ofKepler'sLaws(1)and(2)Newton'sdeductions from Kepler'slaws | 3 | K3(Ap) | Computational learning | Short summary |
|  | 3 | ToderiveKepler'sThird LawfromNewton'slaw ofGravitation, Tofind Themassofaplanet | 4 | K2(U) | Problem solving | Recall steps |
|  | 4 | To <br> fixthepositionofaplanetin itselliptic orbit, Geocentric andHeliocentric latitudesandlongitudes | 4 | K4(An) | LectureIllustration | FormativeTest, OnlineQuiz |


|  | 5 | To prove that theHeliocentriclongitudeof the Earth andGeocentric longitudeof the Sun differ by $180^{\circ}$ | 4 | K2(U) | Lecturelllustrati | n SlipTest |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V | Two Body Problem |  |  |  |  |  |
|  | 1 | Two Body Problem Introduction, Newton's FundamentalequationofMot ion | 4 | K2(U) | Introductory to Two body Problems | Recall basic definitions |
|  | 2 | Motionofoneparticle relativetoanother | 3 | K3(Ap) | Experimental learning | Evaluation through online quiz |
|  | 3 | The motion of the common center of mass | 3 | K4(An) | Blended learning | FormativeAssessme nt Test II |
|  | 4 | The motion of two particles relative to the common mass center | 4 | K4(An) | Problem solving | Online Assignment |
|  | 5 | The motion of a planetwith respect totheSun | 4 | K2(U) | Lecture using videos | Solving problems |

Course Focusing on Employability/Entrepreneurship/Skill Development : Skill Development

Activities (Em/En/SD): Evaluation through short test, Seminar
Course Focusing on Cross Cutting Issues(Professional Ethics/Human Values/Environment Sustainability/Gender Equity)-Nil

## Assignment:

1.To prove that the Helio centric longitude of the Earth and Geocentric longitude of the Sun differ by $180^{\circ}$
2. The motion of the common center of mass

## Seminar Topic:

Motion of two particles relative to the common mass center.

## Sample questions:

## Part-A

1. The Zenith distance is the complement of the. $\qquad$
2. The observer observes the line of horizon at the point. $\qquad$
3.State True or False: The direction in which the body is seen from the centre of earth is called heliocentric direction.
3. State Kepler's first law
4. Perigee and apogee are together called. $\qquad$
Part - B
5. Write a short note on cardinal points
6. Write a short note on Dip of horizon
7. Derive tangent formula
8. Write a short note on Kepler's third law
15.Derive motion of one particle relative to another
Part - C

## Answer all the questions:

16. Explain about morning and evening stars
17. Find the duration of twilight when it is shortest
18. Derive Cassin's formula for refraction
19.Explain interpretation of Newton's laws
20.Explain about Eclipses of sun


Head of the Department
Dr.S. KAVITHA


Course Instructor
Dr.Y.A.SHINY

